

## Chapter # 9

### Problem # 9-1

Take the following data to estimate the difference between the fluid thermodynamic pressure and turbulent effective pressure; for the air flow through the wind tunnel, the pressure of the air is 1 bar, the average velocity is  $u = 50$  m/s, the temperature of air is  $20^\circ\text{C}$ , and turbulence intensity  $\sqrt{u'^2} / u = 5\%$ , (which is a quite large value). Assumed that the turbulence is isotropic, i.e. various statistical values regardless of the direction of turbulence, here is  $\overline{u'^2} = \overline{v'^2} = \overline{w'^2}$

### Problem # 9-2

Try to write k equation in three dimension Cartesian coordinates (see 9-21)

### Problem # 9-4

In a two-dimensional boundary layer flow, if the generation of turbulent kinetic energy and dissipation balanced each other, try this

$$\sqrt{\tau_w / \rho} = C_\mu^{1/4} k^{1/2}.$$

### Problem # 9-5

The definition of turbulent kinetic energy dissipation rate is  $\varepsilon = \nu \overline{\left(\frac{\partial u'_i}{\partial x}\right)^2}$ . Try to write the expression of  $\varepsilon$  in three dimension Cartesian coordinates, and identify its dimension and unit (SI). Then to analyze  $c_\mu, c_1, c_2$  are dimensionless numbers or not.