## Numerical Heat Transfer

（数值传热学）
Chapter 6 Primitive Variable Methods for Elliptic Flow and Heat Transfer（2）


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### 6.4 Approximations in SIMPLE Algorithm

### 6.4.1 Calculation procedure of SIMPLE algorithm

1. Assuming initial velocity fields, $u^{0}$ and $v^{0}$, to determine the coefficients of momentum equations;
2. Assuming an initial pressure field, $p^{*}$;
3. Solving discretized momentum equation based on $p^{*}$, obtaining $u^{*}, \nu^{*}$;
4. Solving pressure correction equation, obtaining $p^{\prime}$;
5. Revising pressure and velocities by $p^{\prime}: p=p^{*}+\alpha_{p} p^{\prime}$

$$
u=u_{e}^{*}+u_{e}^{\prime}=u_{e}^{*}+d_{e} \Delta p_{e}^{\prime} \quad v=v_{n}^{*}+v_{n}^{\prime}=v_{n}^{*}+d_{n} \Delta p_{n}^{\prime}
$$

6a．Solving other scalar variables coupled with velocity；
6b．Starting next iteration with $u=u_{e}^{*}+u_{e}^{\prime}, v=v_{n}^{*}+v_{n}^{\prime}$ and $p=p^{*}+\alpha_{p} p^{\prime}$ as the solutions of the flow field at present iteration level．
In the following discussion focus will be paid on the solution of flow field，and Step 6a will be ignored．The entire solution procedure is composed of six steps．
SIMPLE＝Semi－implicit method for pressure－linked equations（求解压力耦合问题的半隐方法）－
where＂semi－implicit＂refers to the neglect of velocity correction effects of the neighboring grids．

## 6．4．2 Approximations in SIMPLE algorithm

SIMPLE is the dominant algorithm for solving incompressible flows．It was proposed in 1972．Since then many variants（方案）were proposed to improve （overcome）following two assumptions．

1．Inconsistency（不一致性）of initial field assumptions
In SIMPLE $u^{0}, v^{0}$ and $p^{*}$ are assumed independently． Actually there is some inherent（固有的）relationship between velocity and pressure；
2．Overestimating（夸大）the effects of pressure correction of the neighboring nodes．Because $u_{\mathrm{e}}$＇is caused by both the pressure correction and velocity corrections of its
neighboring nodes．The neglect of velocity corrections of the neighboring nodes attributes（归结于）the driving force of $u_{\mathrm{e}}$＇totally to pressure correction，thus exaggerating（夸大）the action of pressure correction．

## 6．4．3 Numerical example

［Example 6－1（Text book）］ Known：

$$
\begin{aligned}
& p_{W}, p_{S}, u_{e}, v_{n} \\
& u_{w}=0.7\left(p_{W}-p_{P}\right) \\
& v_{s}=0.6\left(p_{S}-p_{P}\right)
\end{aligned}
$$

Find：$p_{P}, u_{w}, v_{s}$


The key to solve Example 6－1：how to understand ：

$$
u_{w}=0.7\left(p_{W}-p_{P}\right) \quad v_{s}=0.6\left(p_{S}-p_{P}\right)
$$

They should be regarded as follows

$$
\begin{gathered}
a_{e} u_{e}^{*}=\sum a_{n b} u_{n b}^{*}+b+A_{e}\left(p_{P}^{*}-p_{E}^{*}\right) \\
u_{e}^{*}=\frac{\sum a_{n b} u_{n b}^{*}+b}{a_{e}}+\frac{A_{e}}{a_{e}}\left(p_{P}^{*}-p_{E}^{*}\right)=\overline{u_{e}^{*}}+d_{e}\left(p_{P}^{*}-p_{E}^{*}\right)
\end{gathered}
$$

$\begin{aligned} & \text { For this } \\ & \text { example }\end{aligned} u_{w}=0+0.7\left(p_{W}-p_{P}\right) \quad u_{w}^{*}=0 d_{w}=0.7$

$$
\text { Similarly, } d_{s}=0.6
$$

## 6．5 Discussion on SIMPLE and Convergence Criteria of Flow Field Iteration

## 6．5．1 Discussion on SIMPLE algorithm

1．Can the simplification approximations affect the computational results？

2．Mathematically what type does the boundary condition of the pressure correction equation belong to ？

3．How to adopt the underrelaxation method in the flow filed iteration process？

6．5．2 Convergence criteria of flow field iteration

## 6．5 Discussion on SIMPLE and Convergence Criteria of Flow Field Iteration

## 6．5．1 Discussion on SIMPLE algorithm

1．Can the simplification approximations affect the computational results（solution accuracy）？
The approximations of SIMPLE will not affect the converged solution，but do affect the convergence speed for the following reasons：
（1）The inconsistency between $u^{0}, v^{0}, p^{*}$ will be gradually eliminated with the proceeding of iteration（随着迭代的进行）；
（2）The term $\sum u_{n b}^{\prime}$ in $u_{e}^{\prime}$ will gradually approach zero （趋近于0）with the proceeding of iteration if it converges！

2．What type does the boundary condition of the pressure correction equation belong to ？
（1）Mathematically the boundary condition of the pressure correction equation is Newmann condition，
－Gresho＇s question（1991：A simple question to SIMPLE users）

$$
\frac{\partial p^{\prime}}{\partial n}=0
$$

（2）The adiabatic type boundary condition of the pressure correction equation can uniquely（唯一地）define an incompressible flow problem，because pressure exists in the $\mathrm{N}-\mathrm{S}$ equation in terms of gradient！

$$
\begin{aligned}
& \vec{U} \bullet \nabla \vec{U}=-\frac{1}{\rho} \nabla p+v \nabla^{2} \vec{U} \\
& \nabla \bullet \vec{U}=0
\end{aligned}
$$

（3）The boundary condition of the pressure correction equation makes the ABEqs．being linearly dependent（线性相关），and the coefficient matrix is singular（奇异）；In order to get a unique solution the compatibility condition （相容性条件）must be satisfied：the sum of the right terms （右端项）of the ABEqs．should be zero．

$$
\begin{aligned}
& a_{P} p_{P}^{\prime}=a_{E} p_{E}^{\prime}+a_{W} p_{W}^{\prime}+a_{N} p_{N}^{\prime}+a_{S} p_{S}^{\prime}+b \quad \text { Mathematically } \\
& a_{P} p_{P}^{\prime}-\left(a_{E} p_{E}^{\prime}+a_{W} p_{W}^{\prime}+a_{N} p_{N}^{\prime}+a_{S} p_{S}^{\prime}\right)=b \\
& \sum b_{i, j, k}=0 \longrightarrow \begin{array}{l}
\text { Right } \\
\text { Mass conservation of the entire } \\
\text { tomain should be satisfied. }
\end{array}
\end{aligned}
$$

Thus the requirement of mass conservation at each iteration level corresponds to the execution of Neumann boundary condition for the satisfaction of compatibility condition．

In our teaching program RMAX, SSUM represent $b_{\text {max }}$ and $\sum b_{i, j}$, respectively.
(4) Determination of absolute pressure

For Neumann condition, $p$ 'should be determined by computation, rather than specified in advance.

After receiving the converged solution, selecting some point as a reference and using the relative results as output.

3.How to adopt the underrelaxation in solving flow fields?
(1) Underrelaxation of pressure correction $p^{\prime}$ :

$$
p=p^{*}+\alpha_{p} p^{\prime}
$$

$\alpha_{p}$--pressure underrelaxation factor
(2) Underrelaxation of velocity is organized into the solution procedure:

Iteration process is generally expressed as:


The obtained numerical results have already be underrelaxed!

Discussion：Can the direct underrelaxation be used for velocity？

$$
u=u^{*}+\alpha_{u} u^{\prime} \quad \text { No ! ! ! }
$$

Reason：The velocity correction is obtained through mass conservation requirement．Its underrelaxation will violate（破坏）mass conservation condition．Thus incorporating（纳入）the underrelaxation of velocity into solution procedure is necessary！

## 6．5．2 Convergence criteria of flow field iteration

1．Two different iterations
（1）Iteration for solving ABEqs．－Inner iteration

This is the solution procedure for ABEqs．with specified coefficients and source term．Discussed in Chapter 5
（2）Iteration for non－linear problem－Outer iteration

This is the process in which the coefficients and source term are updated．

2．Criteria for terminating inner iteration
The major solution work for flow field is in the $p$＇eqs．．Terminating too early is not in favor of（不利于）mass conservation，while too late is not economic．

Three criteria may be used：
（1）Specify the number of iteration cycles：One cycle means that the dependent variables at all nodes have been updated．－－－－Simple but not rational（合理的）；
（2）Specify a threshold（阈值）for the norm（范数）of residual（余量）of p＇eqs．


Zero if converged
Residual may be negative
（3）Specify a threshold for the ratio of residuals（余量）of p＇equations：

$$
R_{p}^{(k)} / R_{p}^{(0)} \leq r_{p}, r_{p}=0.05 \sim 0.25
$$

3．Criteria for terminating outer iteration
（1）Specify a threshold of relative deviation of some quantity

Remarks：

$$
\left|\frac{N u^{(k+n)}-N u^{(k)}}{N u^{(k+n)}}\right| \leq \varepsilon \quad n=1 \sim 100
$$

The smaller the $\alpha$ ，the smaller the value of $\mathcal{E}$ should be．
（2）Specify thresholds for SSUM and RMAX， respectively ：

$$
\frac{\left|R_{\text {SSUM }}\right|}{q_{m}} \leq \varepsilon_{1} ; \frac{R_{M A X}}{q_{m}} \leq \varepsilon_{2}
$$

$q_{m}$－reference flow rate；For open system the inlet flow rate may be used；for closed system，following
definition may be used：

$$
q_{m}=\int \rho|u| d y
$$

For open system if the mass conservation is forced to be satisfied，then $R_{S U M} / q_{m} \leq \varepsilon_{1}$ can not be used as a convergence criterion．

（3）Relative norm（范数）of mass conservation residual less than an allowed value：

## Remarks ：

$$
\frac{\sqrt{\sum(b)^{2}}}{q_{m}} \leq \varepsilon
$$

Residual of mass conservation is：

$$
b=\frac{\left(\rho_{P}^{0}-\rho_{P}\right) \Delta x \Delta y}{\Delta t}+\left[\left(\rho u^{*}\right)_{w}-\left(\rho u^{*}\right)_{s}\right] A_{e}+\left[\left(\rho v^{*}\right)_{s}-\left(\rho v^{*}\right)_{n}\right] A_{n}
$$ Residual of $p^{\prime}$＇equation is：$\quad\left(a_{P} p_{P}^{\prime}-\sum a_{n b} p_{n b}^{\prime}-b\right)$

（4）Relative norm of momentum equation residual less than an allowed value：

Norm of
$\begin{aligned} & \text { momentum } \\ & \text { equation }\end{aligned}=\left(\sum\left\{a_{e} u_{e}-\left[\sum a_{n b} u_{n b}+b+A_{e}\left(p_{P}-p_{E}\right)\right]\right\}^{2}\right)^{1 / 2}$ residual


Resuming to original dimension

$$
\varepsilon \approx 10^{-3} \sim 10^{-6}
$$

A better criterion is：relative norms of both mass conservation and momentum equation less than allowed values．

## 6．6 Developments of SIMPLE algorithm

6．6．1 SIMPLER－Overcoming $1^{\text {st }}$ assumption of SIMPLE（1980）

6．6．2 SIMPLEC－Partially overcoming $2^{\text {nd }}$ assumption of SIMPLE（1984）

6．6．3 SIMPLEX－Partially overcoming $2^{\text {nd }}$ assumption of SIMPLE（1986）

6．6．4 Comparisons of algorithms

## 6．6 Developments of SIMPLE algorithm

## 6．6．1 SIMPLER－Overcoming $1^{\text {st }}$ assumption of SIMPLE（1980）

1．Basic idea
Pressure field is solved from the assumed velocity field，rather than assumed independently．
$p^{\prime}$ is used to correct velocity，but not pressure．
The improved pressure is solve from updated velocity field．

2．How to get pressure field from given velocity field

$$
\begin{gathered}
u_{e}=\sum \frac{a_{n b} u_{n b}+b}{a_{e}}+\frac{A_{e}}{a_{e}}\left(p_{P}-p_{E}\right) \\
u_{e}=\underline{u}+\left(\frac{A_{e}}{a_{e}}\right)\left(p_{P}-p_{E}\right)=u+d_{e}\left(p_{P}-p_{E}\right) ; v_{n}=\tilde{v}_{n}+d_{n}\left(p_{P}-p_{N}\right)
\end{gathered}
$$

$u_{e}$ is called pseudo－velocity（假拟速度）。
Substituting $u_{e}, v_{n}$ into continuum equation and re－arranging：

$$
\begin{gathered}
a_{P} p_{P}=a_{E} p_{E}+a_{W} p_{W}+a_{N} p_{N}+a_{S} p_{S}+b \\
b=\frac{\left(\rho_{P}^{0}-\rho_{P}\right) \Delta x \Delta y}{\Delta t}+\left[(\rho u)_{w}-(\rho u)_{s}\right] A_{e}+\left[(\rho \tilde{v})_{s}-(\rho \tilde{v})_{n}\right] A_{n}
\end{gathered}
$$

Equations for $a_{E} \sim a_{S}, a_{P}$ are the same as that for $p$＇．
3．Boundary condition of $p$－equation
The same as for $p^{\prime}$ ：zero coefficients of boundary

## 4．Calculation procedure of SIMPLER

（1）Asuuming initial field $u^{0}, v^{0}$ ，determining coefficient， b and pseudo－velocity $u, v$ ；
（2）Solving pressure equations，and taking the results as $p$＊；
（3）Solving discretized momentum equations ，and taking the results as $u^{*}, \nu^{*}$ ；
（4）Solving pressure correction equations，yielding $p^{\prime}$ ；
（5）Correcting velocity from $p^{\prime}$ ，yielding $u^{\prime}, v^{\prime}$ ；
（6）Taking $\left(u^{*}+u^{\prime}\right),\left(v^{*}+v^{\prime}\right)$ as the flow solution of the present level and starting iteration for next level．

## 5．Discussion on SIMPLER algorithm

## SIMPLER＝SIMPLE REVISED－Patankar（1980）

（1）At each iteration level two pressure equations are solved，hence more computational time is needed for each iteration．However，the improved consistency between initial flow and pressure fields makes the total iteration times often shorter．
（2）In SIMPLER no any effort is taken to overcome the $2^{\text {nd }}$ assumption；In addition a new inconsistency is introduced：pressure is always determined from the previous flow field．

### 6.6.2 SIMPLEC - Partially overcoming the $2^{\text {nd }}$ assumption (1984)

## 1.Basic idea

In SIMPLE some inconsistency is introduced when neglecting the velocity correction term of neighbour nodes :neglecting $\sum a_{n b} u_{n b}^{\prime}$ is equivalent to let $a_{n b} \rightarrow 0$, while in the main diagonal term, i.e, in $a_{P}=\sum_{n b}^{n b} a_{n}-S_{P} \Delta V$ no any correspondent action is taken.
2. A more consistent treatment

At the two sides of the $u^{\prime}-p^{\prime}$ equation

$$
a_{e} u_{e}^{\prime}=\sum a_{n b} u_{n b}^{\prime}+A_{e}\left(p_{P}^{\prime}-p_{E}^{\prime}\right)
$$

subtracting the term $\sum a_{n b} u_{e}^{\prime}$ from both sides yielding:

$$
a_{e} u_{e}^{\prime}-\sum a_{n b} u_{e}^{\prime}=\sum a_{n b}\left(u_{n b}^{\prime}-u_{e}^{\prime}\right)+A_{e}\left(p_{P}^{\prime}-p_{E}^{\prime}\right)
$$

$$
u_{e}^{\prime}\left(a_{e}-\sum a_{n b}\right)=\sum a_{n b}\left(\dot{y}_{n b}^{\prime}-u_{e}^{\prime}\right)+b+A_{e}\left(p_{P}^{\prime}-p_{E}^{\prime}\right)
$$

It can be expected that：$u_{e}, u_{n b}^{\prime}$ are in the same order of magnitude,$\sum a_{n b}\left(u_{n b}^{\prime}-u_{e}^{\prime}\right)$ is much smaller than other terms at right side，hence effect of neglecting it will be much smaller that that of neglecting $\sum a_{n b} u_{n b}^{\prime}$ in SIMPLE algorithm．

$$
\begin{array}{cc}
u_{e}^{\prime}=\left(\frac{A_{e}}{a_{e}-\sum a_{n b}}\right)\left(p_{P}^{\prime}-p_{E}^{\prime}\right) & v_{n}^{\prime}=\left(\frac{A_{n}}{a_{n}-\sum a_{n b}}\right)\left(p_{P}^{\prime}-p_{N}^{\prime}\right) \\
d_{e} & d_{n}
\end{array}
$$

This is velocity correction equation in SIMPLEC．
3．Calculation procedure of SIMPLEC
The same as SIMPLE with following two different
(1) The $d$ term in velocity correction equation is:

$$
d_{e}=\frac{A_{e}}{a_{e}-\sum a_{n b}} ; d_{n}=\frac{A_{n}}{a_{n}-\sum a_{n b}}
$$

(2) No underrelaxation for $p^{\prime}$.
4. The denominator in $d$ will never be zero

Because the underrelaxation of flow field is organized into the solution procedure, the coefficient $a_{e}, a_{n}$ in the above equations are actually $a_{e} / \alpha_{e}$ and $a_{n} / \alpha_{n}$, respectively! Hence $\left(a_{e} / \alpha_{e}-\sum a_{n b}\right)>0$
5. Discussion on SIMPLEC algorithm

## SIMPLEC＝SIMPLE CONSISTENT，van Doormaal， Raithby（1984）

（1）Through simply improving the coefficient $d$
SIMPLEC partially overcomes the $2^{\text {nd }}$ assumption in SIMPLE without introducing additional computational work ；
（2）Algorithm comparison shows that at a finer grid system SIMPLEC is more efficient．
（3）The inconsistency of initial fields assumption still exists in SIMPLEC．

### 6.6.3 SIMPLEX algorithm

## 1. Basic idea of SIMPLEX (1986, Raithby)

The essential step in SIMPLEC is the improvement of d :

$$
d_{e}=\frac{A_{e}}{a_{e}-\sum a_{n b}} ; d_{n}=\frac{A_{n}}{a_{n}-\sum a_{n b}}
$$

Extending this idea: If a set of algebraic equation of $d$ can be formed which can take the effects of neighboring nodes into consideration, the iteration may be speeded up
2 . Derivation of $d$-equation
Taking following equation in SIMPLE

$$
u_{e}^{\prime}=d_{e}\left(p_{P}^{\prime}-p_{E}^{\prime}\right)=d_{e} \Delta p_{e}^{\prime}
$$

as a general expression，then
introducing：$u_{n b}^{\prime}=d_{n b} \Delta p_{n b}^{\prime}$
and substituting into：$a_{e} u_{e}^{\prime}=\sum a_{n b} u_{n b}^{\prime}+A_{e}\left(p_{P}^{\prime}-p_{E}^{\prime}\right)$
Yielding $\quad a_{e} d_{e} \Delta p_{e}^{\prime}=\sum a_{n b} d_{n b} \Delta p_{n b}^{\prime}+A_{e} \Delta p_{e}^{\prime}$
Assuming that $\quad \Delta p_{e}=\Delta p_{n b}$ A new assumption！
Then：$\quad a_{e} d_{e} \Delta \bar{f}_{e}^{\prime}=\sum a_{n b} d_{n b} \Delta \boldsymbol{p}_{n b}+A_{e}\left\langle p_{e}^{\prime}\right.$

$$
a_{e} d_{e}=\sum a_{n b} d_{n b}+A_{e} \quad \text { ABEqs. for } \mathrm{d}!
$$

From known coefficients of momentum equations d can be solved．

No neighboring nodes were neglected but a new assumption was introduced $\quad \Delta p_{e}^{\prime}=\Delta p_{n b}^{\prime}$

Boundary condition for d ：Zero coefficients of BNNs．
3．Calculation procedure of SIMPLEX
（1）Assuming initial $u^{0}, v^{0}$ ，calculating coefficients and，$b$
（2）Assuming pressure field $p$＊；
（3）Solving discretized momentum equations， yielding $u^{*}, v^{*}$ ；
（4）Solving $d$ equations，and pressure correction equations，yielding $p^{\prime}$ ；
（5）Correcting velocity from $p^{\prime}$ ，yielding $u^{\prime}, v^{\prime}$ ；
（6）Taking $(u *+u '),\left(v *+v^{\prime}\right),\left(p *+p^{\prime}\right)$ as the solutions of the present level and starting the iteration for the next level（ $p$＇is not under－ relaxed．）．

## 6．6．4 Comparisons of algorithms

1．Comparison contents
Convergence rate，and robustness（健壮性，鲁棒性）
2．Comparison methods
（1）Adopting graph of $\alpha_{u} \sim \alpha_{p} \quad \begin{aligned} & \text {－heavy } \\ & \text { computational work }\end{aligned}$

（2）Adopting time step multiple E （时步倍率）～iteration time graph（20211102）

The time step multiple， E ，is defined as：

$$
E=\frac{\alpha}{1-\alpha}
$$

$$
\alpha: 0 \rightarrow 1
$$

$$
E: 0 \rightarrow \infty
$$

It greatly extends the variation range of under－relaxation treatment．

| $\alpha$ | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 | 0.95 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| E | 0.111 | 0.25 | 0.428 | 0.66 | 1 | 1.5 | 2.33 | 4 | 9 | 19 |

$$
\alpha=0.999 \quad E=999
$$

3．Comparison conditions
For comparison results being meaningful，it should be conducted under following conditions：（1）The same grid system；（2）The same convergence criteria； （3）The same discretization scheme；（4）The same solution method for the ABEqs．；（5）The same underrelaxation factors；（6）The same initial fields

4．Remarks
In the comparison of algorithm，the solution and its order of accuracy are the same for all compared algorithms，i．e．，different algorithm should have the same numerical results．Algorithm comparison only relates to

And the comparison of schemes relates to numerical accuracy and computational time. Roughly speaking: :
"Algorithm relates to convergence rate, and scheme to solution accuracy".

## 5.Comparison four examples between SIMPLE, SIMPLER, SIMPLEC, SIMPLEX

(1) The four problems compared

(1)lid-driven cavity flow

(2)flow in a tube with sudden expansion

(3)natural convection
in a square cavity

(4)natural convection in a horizontal annular

## （2）Comparison results（for Problem 3）



## （3）About $d \quad u^{\prime}=d\left(\Delta p^{\prime}\right)$ For a certain correction： $d \uparrow \Delta p^{\prime} \downarrow$

Natural convection in a square cavity

| $42 \times 42$ |  |  |  |  |  | $82 \times 82$ |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | SIMPLE | SIMPLER | SIMPLEX | SIMPLEX | SIMPLE | SIMPLER | SIMPLEX | SIMPLEX |  |  |  |
| $d_{u}(10,6)$ | 0.5927 | 0.5927 | 2.964 | 2.928 |  | 0.2981 | 0.2981 | 1.490 | 1.474 |  |  |
| $d_{u}(20,20)$ | 0.5960 | 0.5960 | 2.980 | 2.979 |  | 0.2975 | 0.2975 | 1.488 | 1.488 |  |  |

Natural convection in a square cavity
 Thus in SIMPLEC，SIMPLEX no underrelaxation

Zeng M, Tao W Q. A comparison study of the convergence characteristics and robustness for four variants of SIMPLE family at fine grids. Engineering Computations, 2003, 20(3/4):320-341

### 6.6.5 IDEAL algorithms

## IDEAL algorithm have completely overcome the two assumptions of SIMPLE algorithm.

1. Sun DL, Qu Z G, He Y L, Tao WQ. An efficient segregated algorithm for incompressible fluid flow and heat transfer problems-IDEAL (Inner doubly iterative efficient algorithm for linked equation) Part I:mathematical formulation and solution. Numerical Heat Transfer, Part B, 2008,53(1);1-17
2. Sun DL, Qu Z G, He Y L, Tao WQ. An efficient segregated algorithm for incompressible fluid flow and heat transfer problems-IDEAL (Inner doubly iterative efficient algorithm for linked equation) Part II:Application examples. Numerical Heat Transfer, Part B, 2008,53(1);18-38

2-D DEAL code can be found in our website.

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